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Econ 842 International Monetary Economics

> PROBLEM SET 2 - EXCHANGE RATES (Due February 20)

1. This question is based on the monetary model of exchange rate determination. Equilibrium in the domestic and foreign money markets is given by (with all variables in logs, except the interest rate).

$$\begin{array}{rcl} m_t - p_t &=& \phi y_t - \lambda i_t \\ m_t^* - p_t^* &=& \phi y_t^* - \lambda i_t^* \end{array}$$

where ϕ is the income elasticity of money demand and λ is the interest rate semielasticity of money demand. Money demand parameters are identical across countries. International capital market equilibrium is given by uncovered interest parity:

$$i_t - i_t^* = E_t s_{t+1} - s_t$$

where $E_t s_{t+1}$ is the expectation at time-t of the exchange rate in period t + 1. Price levels and the exchange rate are related through purchasing-power parity:

$$s_t = p_t - p_t^*$$

Define $f_t = (m_t - m_t^*) - \phi(y_t - y_t^*)$ as the economic fundamentals.

- (a) Derive a first-order stochastic difference equation for the equilibrium exchange rate, s_t .
- (b) Find the fundamentals (no bubbles) solution. What is the condition for this solution to hold?
- (c) Consider the effect of an unanticipated announcement at date t = 0 that the money supply is going to permanently rise on a future date T, i.e., $f_t = \bar{f}$ when t < T, and then $f_t = \bar{f} + \Delta$ for $t \ge T$. Derive the path of exchange rate and show the path in a graph.
- (d) Suppose that the fundamentals are governed by a stationary AR(1) process, $f_t = \rho f_{t-1} + \epsilon_t$, where ϵ_t is an i.i.d. shock. Show and discuss how the persistence of fundamentals affect the volatility of the exchange rate.

Prof. Kasa Spring 2007 2. Consider the following present value model of exchange rate determination:

$$s_t = (1 - \beta) \sum_{j=0}^{\infty} \beta^j E(f_{t+j} | \Omega_t) \qquad 0 < \beta < 1$$

where s_t is the log exchange rate, f_t is the log of fundamentals, and Ω_t is the information set at time-t.

Assume fundamentals follow a random walk,

$$f_t = f_{t-1} + \varepsilon_t$$

and assume $var(\epsilon_t) = 1$.

Clearly, if Ω_t contains only f_t and its lags, the solution for the exchange rate is just $s_t = f_t$. Suppose, however, that Ω_t contains f_{t+1} as well as (f_t, f_{t-1}, \ldots) . In other words, agents get a noiseless, one-period ahead signal of the fundamentals.

- (a) Solve for s_t in terms of f_t and f_{t+1} .
- (b) Calculate the variance of $s_t s_{t-1}$. Is the variance bigger or smaller than in the case where Ω_t only contains f_t and its lags?
- (c) Calculate the covariance of $s_t s_{t-1}$ with $f_t f_{t-1}$.
- (d) Now square the answer in part (c), and divide by your answer in part (b). That is, compute $[cov(\Delta s_t, \Delta f_t)]^2/var(\Delta s_t)$. Note, that this is just the squared correlation between Δs_t and Δf_t , since by assumption the variance of $\Delta f_t = 1$. How does this model help to explain the observation that exchange rates are 'disconnected' from fundamentals?
- (e) Engel and West (JPE, 2005) prove a theorem that says exchange rates are unforecastable under certain circumstances, even though fundamentals are forecastable. How does their theorem apply to this model?
- 3. Pick a country, and using the Campbell-Shiller methodology, test the monetary model of exchange rate determination. Define the fundamentals to be $f_t = m_t - m_t^* - (y_t - y_t^*)$, where m and y are logs of the money supply and (real) GDP. (Notice that you can just set the income elasticity of money demand to one). First, plot f_t against s_t . Next, test whether f_t has a unit root, and based on the results, estimate a VAR in either (s_t, f_t) or $(s_t - f_t, \Delta f_t)$. Following the discussion in Engel and West (JPE, 2005), set the discount factor, β , to 0.96. Report tests of the implied cross-equation restrictions, and then plot the actual exchange rate (or the spread, $s_t - f_t$, if fundamentals have a unit root) against the predicted exchange rate (or spread). Finally, check whether exchange rates Granger Cause fundamentals. How do your results here compare to Engel and West's?