



# An Overview and Comparison of Analytical TCP Models

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# Road map

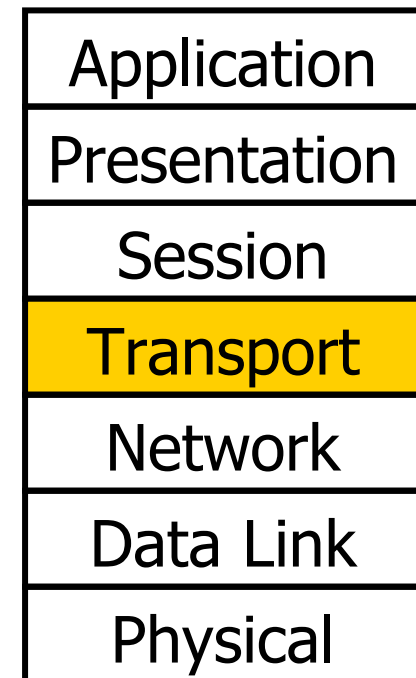
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- Introduction
- Motivation and objectives
- Overview of TCP mechanisms
- Model classification criteria
- Survey a set of analytical models
- Model comparison
- Summary and conclusions



# Introduction

- Transmission Control Protocol (TCP) is a transport protocol
- TCP provides a reliable connection-oriented data service in packet-switched networks.
- Applications: WWW, E-mail, file transfer, remote login, database access, X-windows



OSI Model



# Motivation and Objective

- Most network traffic is carried by TCP
- Analytical models help: evaluate TCP implementations, investigate TCP interaction with queue management algorithms, and define TCP-friendly behaviour
- Objectives:
  - examine the TCP modelling environment
  - compare several analytical TCP models
  - identify the missing features



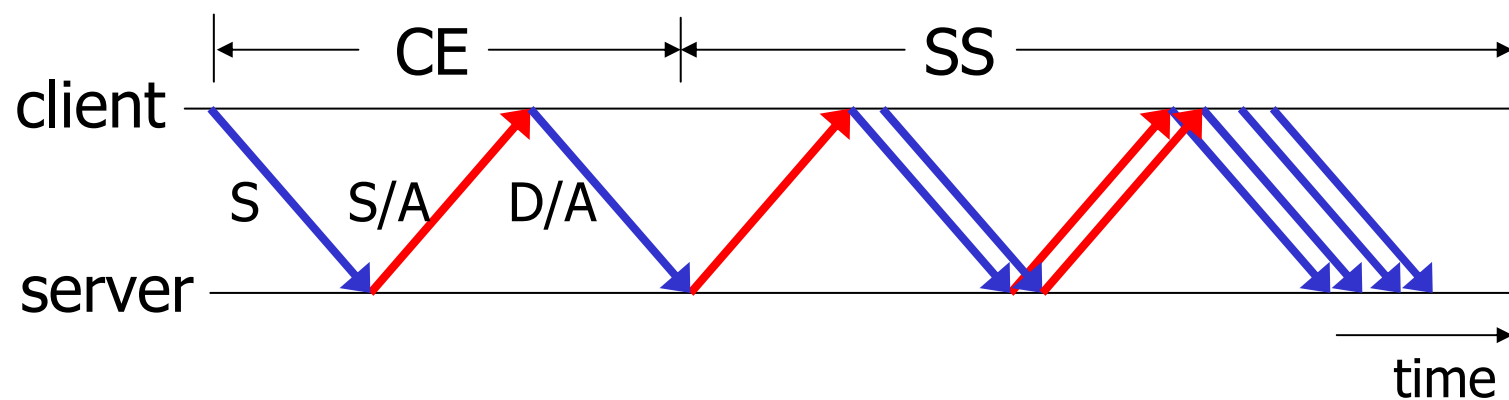
# Overview of TCP

- TCP provides reliable connection-oriented data delivery by employing ACKs, sequence numbers, and timers
- TCP Connection parameters [[RFC 2581](#)]:
  - **cwnd**: sender's congestion window
  - **rwnd**: receiver's advertised window
  - $W_m$ : max. window size,  $\min(\text{cwnd}, \text{rwnd})$
  - **RTT**: round trip time
  - **RTO**: retransmission timeout



# Overview of TCP (cont.)

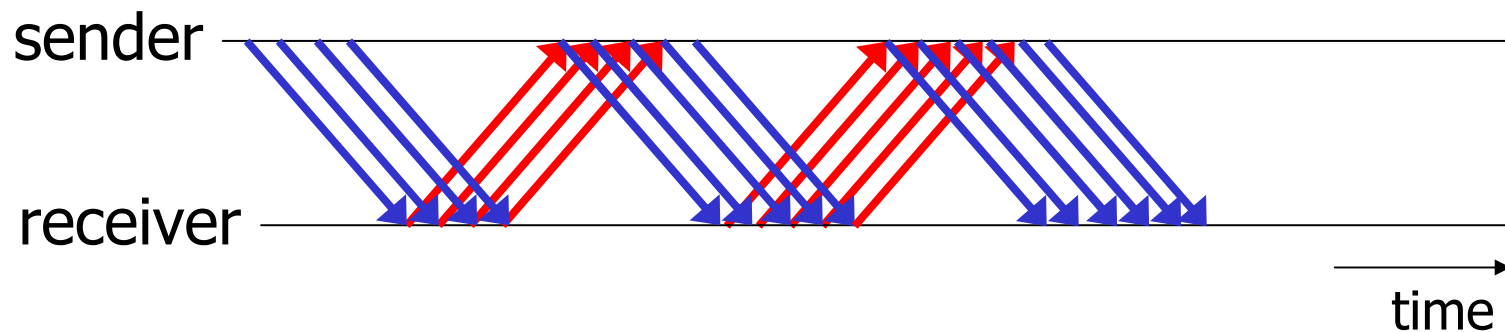
- Connection Establishment (CE):
  - three-way handshake
- Slow Start (SS):
  - increment `cwnd` by **1** for each ACK





# TCP Congestion Control

- **Congestion Avoidance (CA):**
  - switch to CA when **cwnd** reaches **ssthresh**
  - increment **cwnd** by **1** every RTT
  - remain in CA until:
    - TO loss: timeout  $\Rightarrow$  go to SS
    - TD loss: triple duplicate ACKs  $\Rightarrow$  go to FRT





## TCP Congestion Control (cont.)

- **Fast Retransmit** and **Fast Recovery**:
  - immediately retransmit the lost segment
  - set  $ssthresh = cwnd/2$
  - set  $cwnd = ssthresh + 3$  (inflation)
  - transmit a new segment if allowed
  - for each DUPACK: increment  $cwnd$  by 1
  - when ACK for new data arrives, set  $cwnd = ssthresh$  (deflation)

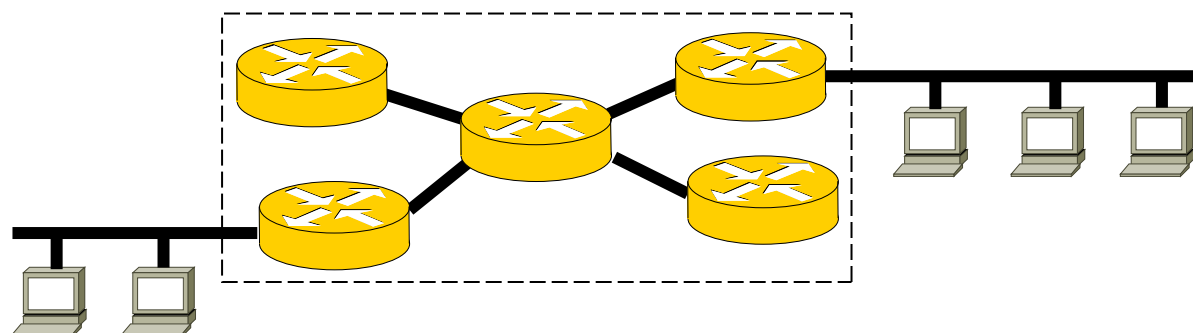




# Delayed Acknowledgement

- TCP receiver may send one ACK for  $b$  segments,  $b \geq 1$  [RFC 2581]
- ACKs are generated:
  - for at least every second segment
  - within 500 msec of the arrival of an unacknowledged segment
  - for out-of-order segments
  - for segments that fill gaps in the sequence number space

# Model Classification



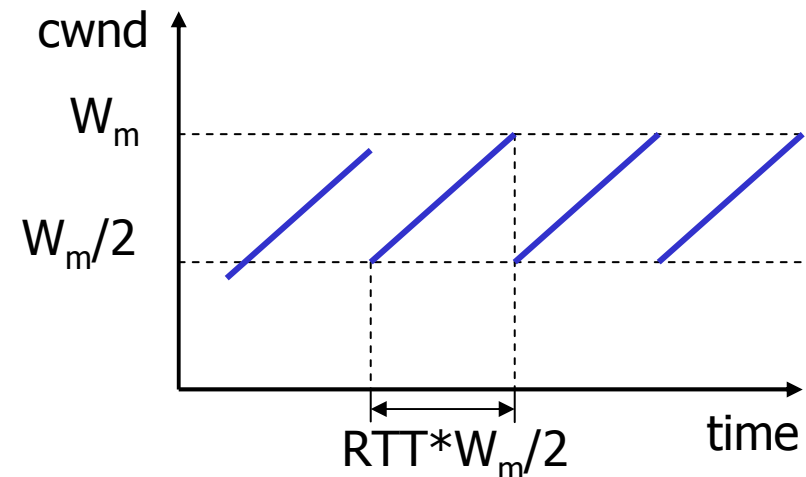
- Three perspectives:
  1. queue dynamics
  2. interaction between TCP and queue management mechanisms
  3. TCP dynamics
- TCP models can be further classified based on transfer length: long, short, or arbitrary



# Models for Long-Lived Transfers

## 1. M. Mathis, et al. (Pittsburgh Supercomputing)

- predict steady-state throughput
- only consider CA phase and TD losses
- periodic loss  $p$
- average throughput:



$$T = \frac{MSS}{RTT} \frac{K}{\sqrt{p}}$$



## Models for Long-Lived Transfers (cont.)

### 2. J. Padhye, et al. (Univ. of Massachusetts)

- predict steady-state throughput
- consider TD and TO losses during CA
- use rounds (round duration=RTT)
- bursty loss model
- average throughput is:

$$T = \min \left( \frac{W_m}{RTT}, \frac{1}{RTT \sqrt{\frac{2bp}{3}} + RTO_0 \min(1, 3\sqrt{\frac{3bp}{8}}) p (1 + 32p^2)} \right)$$



## Models for Transfers of Arbitrary Length

### 3. N. Cardwell, et al. (Univ. of Washington)

- extend **model 2** to include CE and SS
- predict the expected latency  $L$
- CE latency:

$$E[L_{CE}] = RTT + RTO_0 \left( \frac{1 - p_r}{1 - 2p_r} + \frac{1 - p_f}{1 - 2p_f} - 2 \right)$$

- expected latency:

$$E[L] = E[L_{ss}] + E[L_{loss}] + E[L_{ca}] + E[L_{delay}]$$



# A Model for Short-Lived Transfers

## 4. M. Mellia, et al. (Turin Polytechnic)

- use CE latency from **model 3**
- compute average L by exhaustively enumerating all loss scenarios:

$$\begin{aligned} L_1^1 &= RTT + q \sum_{i=1}^{\infty} p^i \sum_{j=1}^i 2^{j-1} RTO \\ &= RTT + RTO \frac{p}{1-2p} \end{aligned}$$

- only handles transfers of a few segments, because complexity grows exponentially



# Model Comparison

- Common assumptions:
  - no specific topology or queue management
  - greedy sources ([Mathis](#))
  
- Common features:
  - using rounds ([Padhye](#))
  - bursty loss model ([Padhye](#))
  - three-way handshake latency ([Cardwell](#))
  - closed-form solutions
  - $L(T)$  is directly (inversely) proportional to  $RTT$ ,  $p$ ,  $RTO$ , and  $E[t_{TO}]$



# Model Validation

Model	Simulation	Controlled measurements	Live measurements	Compare to
Mathis	✓	✓	✗	none
Padhye	✓	✓	✗	none
Altman	✗	✓	✗	Padhye
Cardwell	✓	✓	✓	Mathis, Padhye
Sikdar	✓	✗	✓	Padhye, Cardwell
Mellia	✓	✗	✗	none





# Summary and Conclusions

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- Presented an overview of TCP dynamics and modelling environment
- Surveyed a number of analytical models
- Compared the models w.r.t. assumptions, approaches, and validation methods
- Missing features:
  - accurate model of delayed ACK and fast recovery
  - need for a reference set of measurements and evaluation metrics



# References

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