

Phys. 101.

Lecture 7.

Friday, Jan. 17, 2003.

Topics Covered: Free-Body Diagram.

Friction.

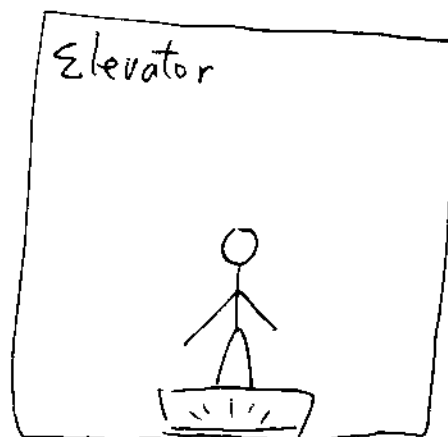
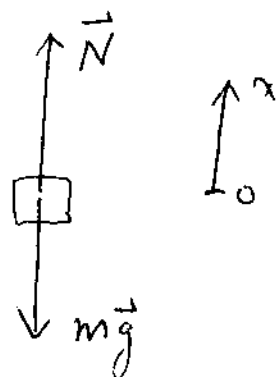
Ref: ch. 5, ch. 6.

- Free-Body Diagram.

1. Isolate the object.
2. Sketch all the forces acting on the object.
3. Set up a coordinate system that's convenient for $\vec{F} = m\vec{a}$.

e.g. How much do you weigh?

Free-Body Diagram



What the scale reads is

$N =$ apparent weight.

Newton's Law: $\vec{F} = m\vec{a}$

$$N - mg = ma$$

$$N = m(a + g)$$

When $a = 0$, $N = mg$. (Apparent weight = weight)

When $a > 0$, $N > mg$.

When $a < 0$, $N < mg$.

When $\underline{a = -g}$, $N = 0$. (Weightless, just like an astronaut in free space.)

↑
Free fall.

i.e., weightless means $N = 0$.

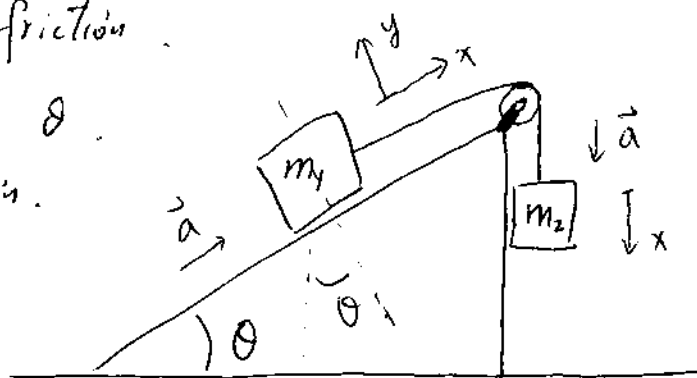
Not $mg = 0$.

7-3.

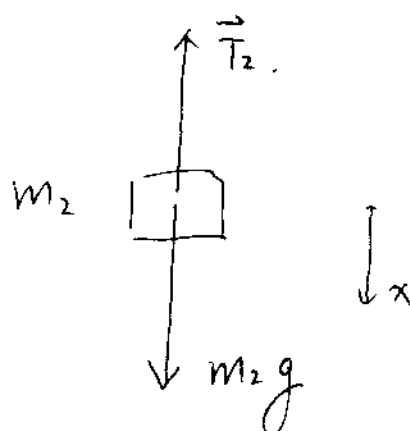
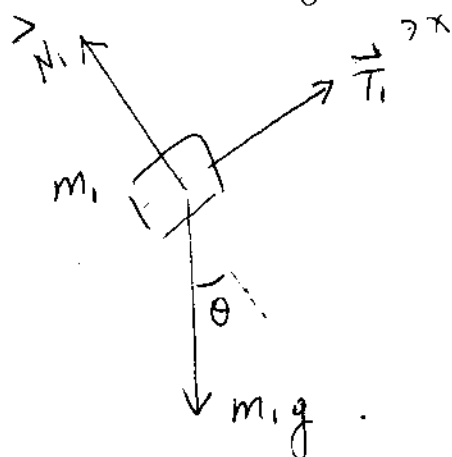
e.g. Assume: No friction.

given: m_1, m_2, θ .

Want: acceleration.



Free-Body Diagrams.



$$|\vec{T}_1| = |\vec{T}_2| = T. \quad (\text{Since No friction})$$

Newton's Law: $\vec{F} = m\vec{a}$.

$$m_1: \quad x\text{-component:} \quad T - m_1 g \sin \theta = m_1 a \quad (1)$$

$$y\text{-component:} \quad N_1 - m_1 g \cos \theta = 0 \quad (2)$$

$$m_2: \quad 1\text{-D:} \quad m_2 g - T = m_2 a \quad (3)$$

3 equations, 3 unknowns.

We can solve for T, a , and N_1 .

• Frictional force . $\vec{f}$

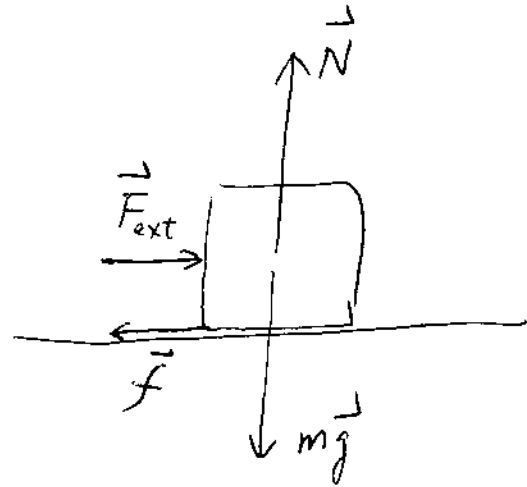
- Occurs at the surface between two objects .

- Due to molecular interaction between the two objects .

- Parallel to the surface .

- Against the relative motion — Kinetic friction

OR. against the tendency of relative motion — static friction .



• Kinetic friction — moving .

$$f = \mu_k \cdot N$$

μ_k — coefficient of kinetic friction .

• Static friction — NOT moving .

$$f \leq \mu_s N, \quad f_{\max} = \mu_s N$$

usually $\mu_s > \mu_k$.

- When F_{ext} is small.

i.e., $F_{\text{ext}} \leq \mu_s N$

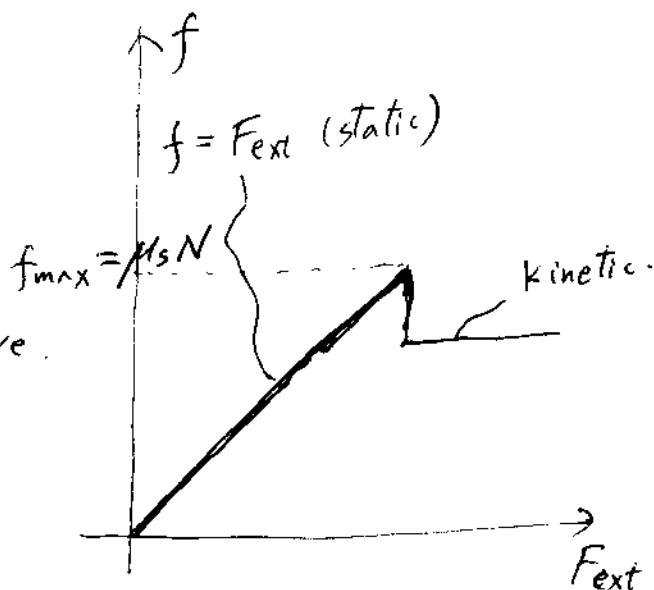
Then, $f = F_{\text{ext}}$.

$F = ma = 0$, object not move.

- When $F_{\text{ext}} > \mu_s N$

Object will move.

$f = \mu_k \cdot N$ (kinetic friction)



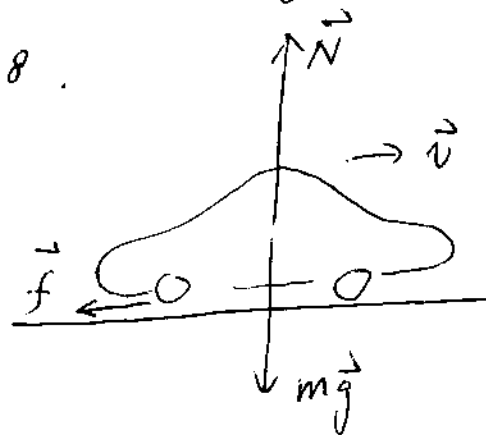
e.g.: Friction between the road and Tires of a car.

$\mu_s = 1.0$, $\mu_k = 0.8$.

If the car is moving at 100 km/h.

how long does it take to stop?

$U_0 = 100 \text{ km/h} = 28 \text{ m/s}$.



Assume wheels are not rolling. (The car skids).

$f = \mu_k N = \mu_k \cdot mg$ (Note: $N = mg$ $\because a_y = 0$).

$a = \frac{f}{m} = \mu_k g = 0.8 \times 9.8 = 7.8 \text{ m/s}^2 = \text{const.}$

$\Delta t = \frac{\Delta U}{a} = \frac{28 \text{ m/s}}{7.8 \text{ m/s}^2} = 3.6 \text{ s}.$

• How do you reduce Δt ?

increase f to $f_{\max}$ ($f_{\max} = \mu_s N$) .

i.e., we want the maximum
of static friction

Idea: Let the wheels roll!

ABS — anti-lock
braking system .

