

CHEM 260

Assignment 4

Due Monday 3rd February 2003

13. Which of the following functions are eigenfunctions of the operator d/dx ? Give the eigenvalues where appropriate. (k is a constant.)
- kx^2 $\sin kx$ $(\sin kx + \cos kx)$ e^{kx} e^{kx^2} e^{-ikx}
14. Suppose that the function e^{ax+bx^2} is an eigenfunction of the operator $\frac{d}{dx} + cx$, where a , b and c are constants. How are the constants related? What is the eigenvalue?
15. Explain briefly the meaning of each of the following terms. Use words, diagrams, mathematical equations as appropriate:
- (a) Degeneracy (b) Normalization (c) Expectation value
(d) Boundary condition (e) Separation of variables.
16. Classify the following molecules as spherical top, symmetric top, asymmetric top, or linear: CO_2 , SF_6 , XeF_4 , HCN , NH_3 , PF_5 , C_6H_6 , CH_4 , C_{60} , HCCH , H_2O , SF_4 .
17. (a) Explain why the lines of the microwave spectrum of carbon monoxide are equally spaced.
(b) The spacing between the lines for $^{12}\text{C}^{16}\text{O}$ is 115.3 GHz. Calculate the bond length. Predict the spacing for $^{13}\text{C}^{16}\text{O}$.
18. Given that the bond length of NO is 0.115 nm, calculate the frequency of the 7th line in the rotational spectrum. Give your answer in units of cm^{-1} .