Preliminary Mathematics/Statistics Exam:

NOTE: This quiz is only for information purposes and will NOT be used as part of the examination component.

Be sure to provide the following information on your answer sheet:

- a) Your name; b) The course which was taken to satisfy the mathematical and statistical prerequisite for this course; c) If you are a college or international transfer student, indicate the school which you previously attended.
- 1) Evaluate by providing a numerical solution or simplify the expression where possible, otherwise expand the summation or formula listing all relevant terms:

$$a > \sum_{i=0}^{10} t \qquad b > \ln (\exp[a]) = \log_{e} \{e^{a}\}$$

$$c > \sum_{i=1}^{3} \sigma_{i}^{2} X_{i}^{2} + 2 \sum_{i>j} X_{i} X_{j} \sigma_{ij} \qquad d > \sum_{j=1}^{3} \sum_{i=1}^{3} X_{i} X_{j} \sigma_{ij}$$

$$e > \exp[a] / \exp[bx] = e^{a} / e^{bx} \qquad f > (x + y)^{3}$$

$$g > \ln(1 + x) \text{ for } x \text{ small (How small is small?)}$$

2) Differentiate the function y with respect to the variable x, i.e., evaluate dy/dx:

a)
$$y = \frac{1}{(1+x)^n}$$
 b) $y = \sum_{t=1}^{T} \frac{1}{(1+x)^t}$
c) $y = \ln[x]$ d) $y = \exp[ax] = e^{ax}$

- 3) Provide definitions (mathematical expressions or equations where possible) for the following terms:
- a) sample mean (average) b) sample variance c) sample covariance
- d) var(A + B) ---the variance of a linear combination of two random variables (A and B)
- e) var(cA B) --- where c is a constant and A and B are random variables
- f) correlation coefficient for A and B-- in terms of covariance and standard deviations
- 4) Simplify the following expressions by re-expressing the series as a ratio:

a)
$$1 + x + x^2 + x^3 + x^4 + \dots$$
 for $|x| < 1$ b) $\sum_{i=1}^{T} \frac{1}{\{1 + r\}^t}$