

Due: Friday, November 7th (in class)

## Reminders

Math 708 students must select a presentation topic and a date for the presentation. Please consult me if you have not done this.

## Reading

Chapters 10 and 11. You can skip Section 11.6.

## Problems for Math 408 and Math 708

1. Consider the set

$$X = \{x \in \mathbb{Z}_+^2 \mid 2x + 5y \leq 17, 2x + 2y \leq 11\}.$$

List and represent graphically the set of feasible points. Use this to find a minimal (facet) description of  $\text{conv}(X)$ .

2. Show that the system  $\{x, y \in \mathbb{R}^2 \mid x + y \leq 0, x - y \leq 0\}$  is not TDI, but that if we add the redundant inequality  $x \leq 0$ , the system becomes TDI.

3. Chapter 8 problem 8.

4. Consider the following 0-1 knapsack polyhedron:

$$X = \{x \in B^6 \mid 5x_1 + 3x_2 + 8x_3 + 9x_4 + 13x_5 + 8x_6 \leq 15\}.$$

1. What is the cover inequality corresponding to variables  $\{1, 2, 3\}$ ?

2. What is the dimension of the face of  $P_I = \text{conv}(X)$  represented by this cover inequality?

3. Lift the inequality you found in part (1) in variable 5, and then lift the resulting inequality in variable 6.

5. Chapter 9 problem 3. In part (ii), the first coordinate of the point to be cut is  $\frac{1}{2}$ , in early printings of the text it is misprinted as  $\frac{1}{4}$ .

## Additional Problems for Math 708

6. Consider the stable set formulation from Chapter 9, problem 14. Take the graph  $G$  which consists of a 5-cycle and a single vertex  $v_6$  attached to each vertex of the cycle. Such graphs are sometimes called *wheels*. The 5-cycle inequality is valid for the 5-wheel.

1. What is the dimension of the face induced by the 5-cycle inequality? What is the dimension of the stable-set polytope of the 5-wheel?

2. Lift this face to a facet by adding a term representing the variable  $x_6$  to the inequality.

7. Chapter 8, Problem 14.

8. What are the facets of the symmetric travelling salesman polytope for the complete graph on 5 vertices?