

The following questions involve using the first and second derivatives to sketch curves and verify relative maximums or minimums.

SHORT ANSWER: Show your steps

- 1) If $f(x) = 2x^3 + 3x^2 - 36x + 1$, determine the intervals on which f is increasing and the intervals on which f is decreasing. 1) _____
- 2) Let $f(x) = 3x^5 - 10x^4 + 7x$. Determine the intervals on which f is (a) concave up and (b) concave down. (c) Find the x -values of all inflection points. 2) _____
- 3) Let $y = x^3 - 3x^2 - 9x + 10$. 3) _____
 - (a) Determine y' and y'' .
 - (b) Determine intervals on which the function is increasing; determine intervals on which the function is decreasing.
 - (c) Determine the coordinates of all relative maximum and relative minimum points
 - (d) Determine intervals on which the function is concave up; determine intervals on which the function is concave down;
 - (e) Determine the coordinates of all inflection points.
 - (f) With the aid of the information obtained in parts (a)–(e), give a reasonable sketch of the curve.
- 4) Determine the intervals on which the function is increasing and on which it is decreasing. Also determine the points of relative maxima and relative minima. 4) _____
 $f(x) = (x^2 - 3x + 2)^2$
- 5) If $y = x^3 + 4x^2 - 3x + 4$, use the second-derivative test to find all values of x for which (a) relative maxima occur (b) relative minima occur. 5) _____
- 6) The cost equation for a company is $C(x) = 2x^3 - 15x^2 - 84x + 3100$. Use the second-derivative test, if applicable, to find the relative maxima and the relative minima. 6) _____
- 7) The cost equation for a company is $C(x) = 2x^3 - 39x^2 + 180x + 21,200$. Use the second-derivative test, if applicable, to find the relative maxima and the relative minima. 7) _____
- 8) The demand equation for a monopolist's product is $p = 200 - 0.98q$, where p is the price per unit (in dollars) of producing q units. If the total cost c (in dollars) of producing 8 units is given by $c = 0.02q^2 + 2q + 8000$, find the level of production at which profit is maximized. 8) _____
- 9) The demand function for a monopolist's product is $p = 100 - 3q$, where p is the price per unit (in dollars) for q units. If the average cost $\bar{c}$ (in dollars) per unit for q units is $\bar{c} = 4 + \frac{100}{q}$, find the output q at which profit is maximized. 9) _____
- 10) The demand equation for a monopolist's product is $p = \frac{500}{\sqrt{q}}$, where p is the price per unit (in dollars) for q units. If the total cost c (in dollars) of producing q units is given by $c = 5q + 2000$, then the level of production at which profit is maximized is 10) _____