

PART II: WRITTEN SECTION. **ANSWER ALL QUESTIONS IN EXAM BOOKLETS****FOR QUESTION 3 YOU MUST ALSO FILL IN THE TABLE ON THE QUESTION SHEET (BELOW)**

- 1) Skippy has \$100 in budget. She buys two goods, x and y. Her *Income Elasticity of Demand* for x is zero. The price of y is \$1. When the price of x is \$2 Skippy buys 20 units of x. When the price of x is \$1, she buys 40 units of x. The most she is willing to pay to have the price of x lowered to \$1 is \$25. Based on this information, answer the following:
- If Skippy pays the \$25 fee and the price is lowered to \$1, how many units of x does she consume?
 - Instead of lowering the price of x, you were to give Skippy a lump sum amount that would be as good as having the price of x fall to \$1. How much would you give her and how many units of x will she consume?
 - Show everything you know about this question in a CAREFULLY drawn and labelled graph. Include as much detail as possible. Label both CV and EV
- 2) Suppose there is an industry with two firms. Currently Firm 1 is producing 120 units of Emissions and Firm 2 is producing 60 units of emissions. Each firm's Marginal Savings function (also their Marginal Abatement cost functions) is given by
- $$MS_1 = 120 - E_1.$$
- $$MS_2 = 120 - 2E_2$$

Also, there are four people, each with a marginal damage function $MD_i = (1/3)E_T$ (where $E_T = E_1 + E_2$)

- Find the aggregate MS function
 - Find the aggregate MD function
 - Determine the socially optimal level of emissions E and the MD.
 - Suppose the government decided to use a "Fair" standard that required each firm to produce half of the socially optimal emissions. What would be each firm's MS and total abatement cost?
 - What is the Pigovian tax that would achieve the socially optimal level of emissions? Find each firm's emissions, total abatement costs and tax bill.
 - What are the total social costs of each approach (standard and tax)? Also what is each firm's private costs under each approach?
 - Which option would those damaged by emissions prefer? Explain. What about each firm (1 & 2)? Society as a whole?
- 3) Suppose that the $MD = 5E$ and with its current technology, the firm's MS is given by
- $$MS_1 = 200 - 5E.$$
- Determine the socially optimal level of emissions E .
 - Determine the emissions tax that would achieve the socially optimal level of emissions.

Now suppose the firm can adopt a new technology that changes is MS to

New $MS_2 = 160 - 4E$

Calculate change in all costs for the firm from adopting the new technology when:

- c. The government uses an emissions standard equal to your answer in (a) above
 - d. The government uses an emissions tax equal to your answer in (b)
- (Assume no change to standard or tax rate after the change in technology)

Now suppose the government adjusts the standard and/or the tax such that MD = New MS. Calculate the change in total costs for the firm from adopting the new technology when:

- e. The government adjusts the standard, and
- f. The government adjusts the tax rate

YOU ARE TO SHOW ALL YOUR WORK IN THE BOOKLETS AND FILL IN THE TABLE BELOW

Policy	A Old Technology	B New Tech/old Standard	C New Tech/new Standard
TAC standard	1000	800	986.8

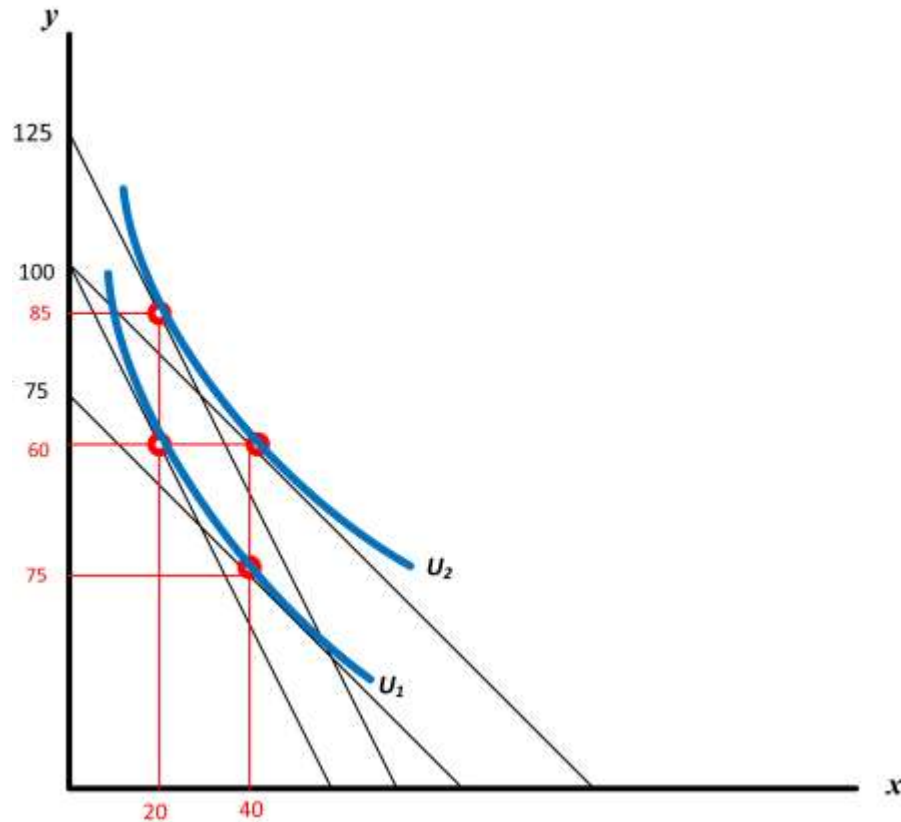
NET CHANGE	Net change (A-B)		Net Change (A-C)
	200		13.2

	Old Technology	New Tech/old tax	New Tech/New Tax
TAC tax	1000	1250	986.8
Tax Bill	2000	1500	1582.4
Total Cost	3000	2750	2569.2

NET CHANGE	Net change (A-B)		Net Change (A -C)
	250		431

ANSWER KEY PART 2

[1] CV and EV: Income Elasticity = 0 for x



Skippy has \$100 in budget. She buys two goods, x and y. Her ***Income Elasticity of Demand*** for x is zero. The price of y is \$1. When the price of x is \$2 Skippy buys 20 units of x. When the price of x is \$1, she buys 40 units of x. The most she is willing to pay to have the price of x lowered to \$1 is \$25. Based on this information, answer the following:

- d. If Skippy pays the \$25 fee and the price is lowered to \$1, how many units of x does she consume?
- e. Instead of lowering the price of x, you were to give Skippy a lump sum amount that would be as good as having the price of x fall to \$1. How much would you give her and how many units of x will she consume?
- f. Show everything you know about this question in a CAREFULLY drawn and labelled graph. Include as much detail as possible. Label both CV and EV

[2] Suppose there is an industry with two firms. Currently Firm 1 is producing 120 units of Emissions and Firm 2 is producing 60 units of emissions. Each firm's Marginal Savings function (also their Marginal Abatement cost functions) is given by

$$MS_1 = 120 - E_1.$$

$$MS_2 = 120 - 2E_2$$

Also, the marginal damage function is given by $MD = (4/3)ET$

(where $ET = E_1 + E_2$)

Find the aggregate MS function

$$E_1 = 120 - MS \quad E_2 = 60 - (1/2)MS$$

$$E_1 + E_2 = ET = 180 - (3/2)MS$$

$$MS = 120 - (2/3)ET$$

Determine the socially optimal level of emissions E and the MD.

$$120 - (2/3)ET = (4/3)ET$$

$$2ET = 120 \quad ET = 60 \quad MD = (4/3)(60) = 80$$

Suppose the government decided to use a "Fair" standard that required each firm to produce half of the socially optimal emissions. What would be each firm's MS and total abatement cost?

$$ET = 60 \quad E_1 = E_2 = 30 \quad MS_1 = 90 \quad MS_2 = 60 \\ TAC_1 = 4050 \quad TAC_2 = 900$$

What is the Pigovian tax that would achieve the socially optimal level of emissions? Find each firm's emissions, total abatement costs and tax bill.

$$\text{Tax rate is } 80 \quad E_1 = 40 \quad E_2 = 20 \\ TAC_1 = (120 - 40)(80)(0.5) = 3200 \quad TAC_2 = (60 - 20)(80)(0.5) = 1600$$

$$\text{Tax Bill} = 3200 \quad \text{Tax Bill} = 1600$$

What is the total social costs of each approach (standard and tax)? Also what is each firm's private costs under each approach?

Standard:

$$\text{Total Abatement costs} = 4050 + 900 = 4950 \quad \text{total Damage} = 2400$$

$$\text{Total social cost is } 7350$$

Tax:

$$\text{Total Damage is } 2400$$

$$TAC_1 = 3200 \quad TAC_2 = 1600 \quad \text{Total Abatement costs} = 4800,$$

$$\text{Tax Bill} = 3200 \quad \text{Tax Bill} = 1600$$

Total Social Cost is 7200**Private Cost: Firm 1: 6400 Firm 2: 3200**

Which option would those damaged by emissions prefer? Explain. What about Each firm (1 & 2)? Society as a whole?

QUESTION 3

Suppose that the $MD = 5E$ and with its current technology, the firm's MS is given by

$$MS_1 = 200 - 5E.$$

- g. Determine the socially optimal level of emissions E .
 $200 - 5E = 5E$, therefore $E = 20$
- h. Determine the emissions tax that would achieve the socially optimal level of emissions.
 $Tax, t = MS = 200 - 5E = 200 - 5(20) = 100$

Now suppose the firm can adopt a new technology that changes its MS to

$$New\ MS_2 = 160 - 4E$$

Calculate change in costs for the firm from adopting the new technology when:

- i. The government uses an emissions standard equal to your answer in (a) above
 If Standard set at $E = 20$, Old Technology has a $TAC = \$1000$. New Technology has $MS = 80$ and a $TAC = 800$. Savings from switching is \$200
- j. The government uses an emissions tax equal to your answer in (b)
 (Assume no change to standard or tax rate after the change in technology)

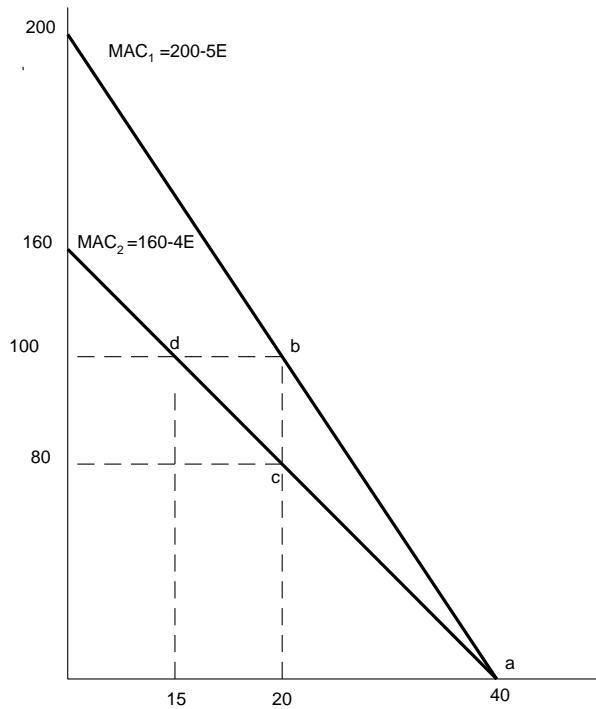
With \$100 tax

$$Old: MS_1 = 200 - 5E = 100\ tax\ E = 20$$

$$New\ MS_2 = 160 - 4E = 100\ tax\ E = 15$$

	Tech 1 (old)	Tech 2 (new)
TAC	$100 \times 20 \times (1/2) = 1000$	$25 \times 100 \times (1/2) = 1250$
TAX Bill	$100 \times 20 = 2000$	$100 \times 15 = 1500$
	\$3000	\$2750

Savings from switching is \$250



Now suppose the government adjusts the standard and/or the tax such that $MD = \text{New MS}$. Calculate the change in total costs for the firm from adopting the new technology when:

- k. The government adjusts the standard, and
- l. The government adjusts the tax rate

Under NEW technology:

$$MS_2 = MD$$

$$160 - 4E = 5E$$

$$E = 17.8 \text{ and } MS = 88.9$$

With a standard equal to 17.8

$$TAC = (40 - 17.8)(88.9) \cdot (1/2) = 986.8$$

$$\text{Savings} = 1000 - 986.8 = 13.2$$

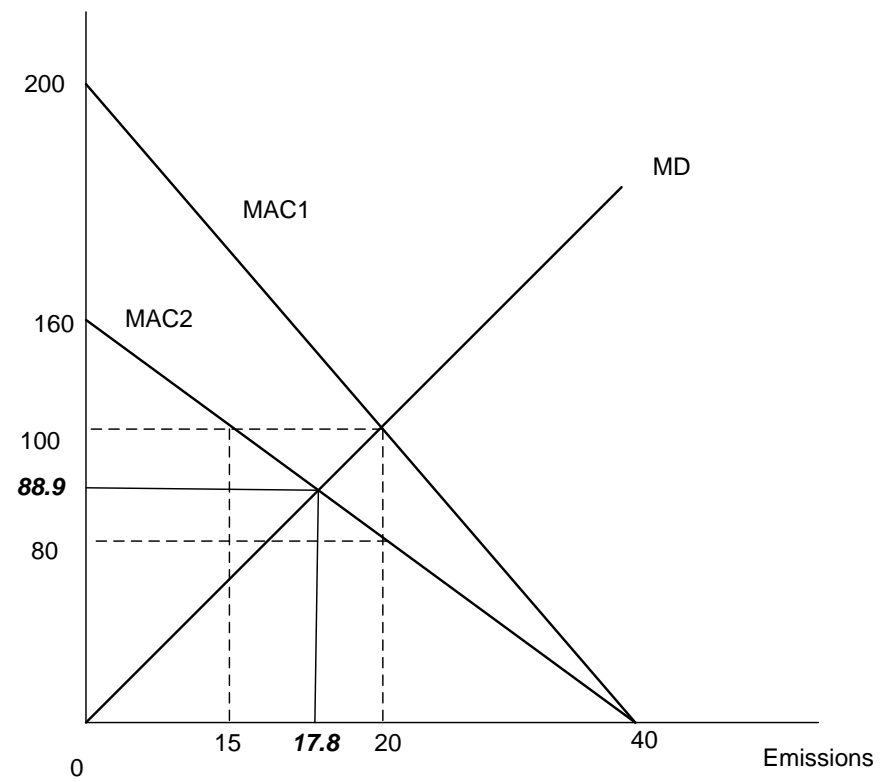
Under Tax rate of $t = 88.9$, $E = 17.8$

$$\text{Tax bill} = (88.9)(17.8) = 1582.4$$

$$\text{And } TAC = 986.8$$

$$TAC + \text{Taxbill} = 2569.2$$

$$\text{Savings} = 3000 - 2569.2 = 430.8$$



Note in Graph: MAC_1 is MS_1 and MAC_2 is MS_2