

Question 1

Suppose that the $MD = 5E$ and with its current technology, the firm's MS is given by

$$MS_1 = 200 - 5E.$$

- Determine the socially optimal level of emissions E.
 $200 - 5E = 5E$, therefore $E = 20$
- Determine the emissions tax that would achieve the socially optimal level of emissions.
 $\text{Tax, } t = MS = 200 - 5E = 200 - 5(20) = 100$

Now suppose the firm can adopt a new technology that changes its MS to

$$\text{New } MS_2 = 160 - 4E$$

Calculate change in costs for the firm from adopting the new technology when:

- The government uses an emissions standard equal to your answer in (a) above
If Standard set at $E = 20$, Old Technology has a TAC = \$1000. New Technology has $MS = 80$ and a TAC = 800. Savings from switching is \$200
- The government uses an emissions tax equal to your answer in (b)
(Assume no change to standard or tax rate after the change in technology)

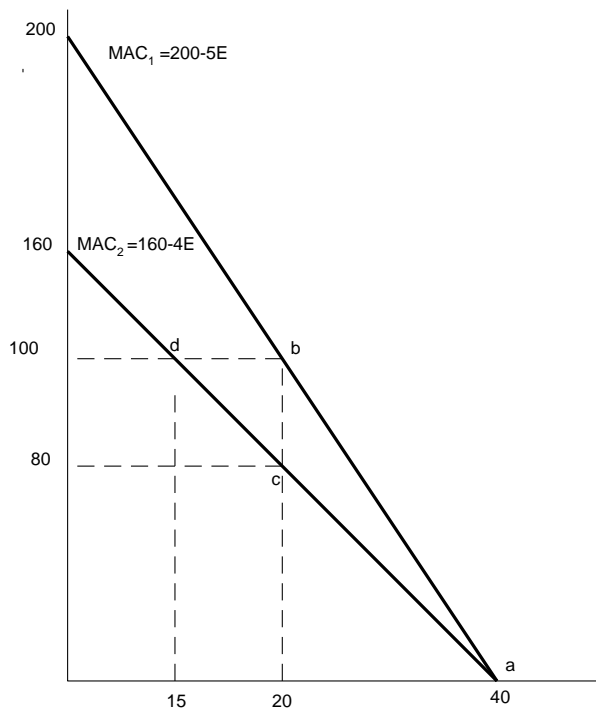
With \$100 tax

$$\text{Old: } MS_1 = 200 - 5E = 100 \text{ tax } E = 20$$

$$\text{New } MS_2 = 160 - 4E = 100 \text{ tax } E = 15$$

	Tech 1 (old)	Tech 2 (new)
TAC	$100 \times 20 \times (1/2) = 1000$	$25 \times 100 \times (1/2) = 1250$
TAX Bill	$100 \times 20 = 2000$	$100 \times 15 = 1500$
	\$3000	\$2750

Savings from switching is \$250



Now suppose the government adjusts the standard and/or the tax such that $MD = \text{New MS}$. Calculate the change in total costs for the firm from adopting the new technology when:

- e) The government adjusts the standard, and
- f) The government adjusts the tax rate

Under NEW technology:

$$MS_2 = MD$$

$$160 - 4E = 5E$$

$$E = 17.8 \text{ and } MS = 88.9$$

With a standard equal to 17.8

$$TAC = (40 - 17.8)(88.9) \cdot (1/2) = 986.8$$

$$\text{Savings} = 1000 - 986.8 = 13.2$$

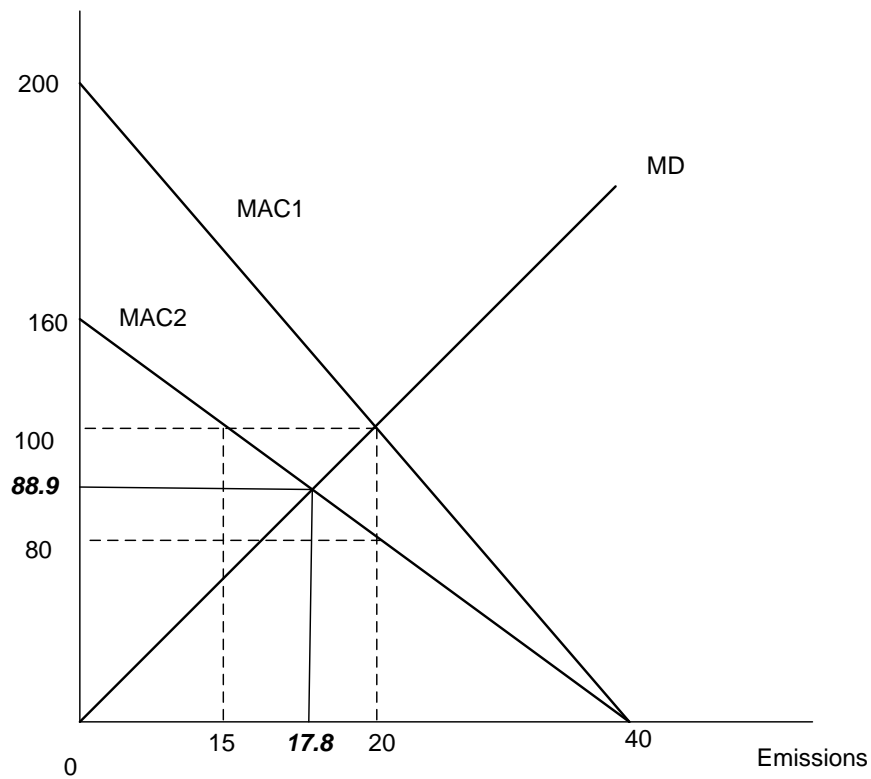
Under Tax rate of $t = 88.9$, $E = 17.8$

Tax bill = $(88.9)(17.8) = 1582.4$

And TAC = 986.8

TAC + Taxbill = 2569.2

Savings = $3000 - 2569.2 = 430.8$



Note in Graph: MAC_1 is MS_1 and MAC_2 is MS_2

Question 2

- a) Aggregating the MS's

$$MS_1 = 120 - E_1 \quad MS_2 = 96 - .8E_2 \quad MS_3 = 160 - 1.33E_3$$

Re-write as

$$E_1 = 120 - MS \quad E_2 = 120 - 1.25MS \quad E_3 = 120 - 0.75MS$$

$$E^T = E_1 + E_2 + E_3 = 360 - 3MS \quad \text{or} \quad MS = 120 - 1/3E$$

- b) Social Optimum is $MD = MS$ or $E^* = 120$
 c) Uniform standard: $E_1 = E_2 = E_3 = 40$ $MS_1 = 80, MS_2 = 64, MS_3 = 106.8$

$$TAC_1 = 3200 \quad TAC_2 = 2560 \quad TAC_3 = 4272$$

- d) Tax is found where
- $MD(120) = (2/3)(120) = 80$

$$E_1 = 40, E_2 = 20, E_3 = 60$$

TAC for each is:

$$TAC_1 = \$3,200$$

$$TAC_2 = \$4,000$$

$$TAC_3 = \$2,400$$

- e) For Marketable Permits the Equilibrium price will be \$80 (Same as the tax). The emissions and total abatement costs will be the same as the tax case. However, their NET total cost will differ, depending if they are net buyers or sellers:

		Allocated Permits	Buy or Sell
Firm 1	$E = 40$	40	0
Firm 2	$E = 20$	40	-20
Firm 3	$E = 60$	40	+20

Permit Costs (negative if net seller)			Net Total costs (TAC & Permits bought/Sold)	
TAC1	\$3,200	Permits1 \$0	TC 1	\$3,200
TAC2	\$4,000	Permits2 -\$1,600	TC 2	\$2,400
TAC3	\$2,400	Permits3 \$1,600	TC 3	\$4,000

Emissions		Uniform Standard	Optimal Tax = 80	Permits Price = 80	Allocated Permits
E1		40	40	40	40
E2		40	20	20	40
E3		40	60	60	40
MAC's					
MAC1		\$80	\$80	\$80	
MAC2		\$64	\$80	\$80	
MAC3		\$107	\$80	\$80	
TAC's					
TAC1		\$3,200	\$3,200	\$3,200	
TAC2		\$2,560	\$4,000	\$4,000	
TAC3		\$4,267	\$2,400	\$2,400	
Permit Costs (neg if net seller)					
Permits1				\$0	
Permits2				-\$1,600	
Permits3				\$1,600	
Net Total costs (TAC & Permits bought/Sold)					
TC 1				\$3,200	
TC 2				\$2,400	
TC 3				\$4,000	