

## pg 259 #1 (chapter 12)

$$MS_1 = 5 - e_1 \quad MS_2 = 8 - 2e_2$$

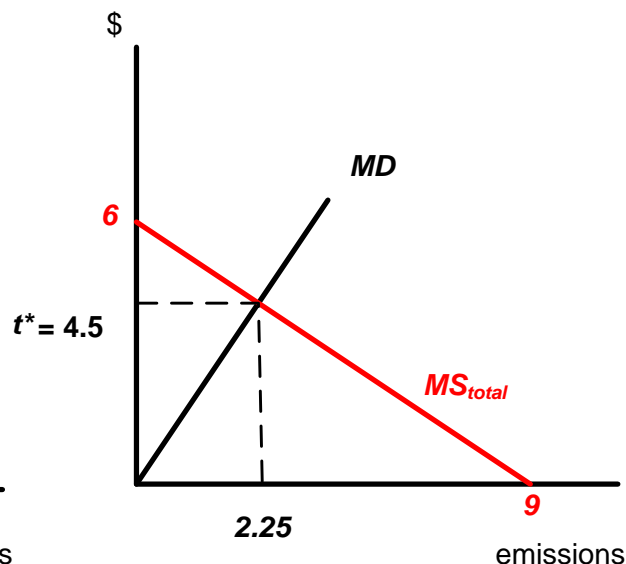
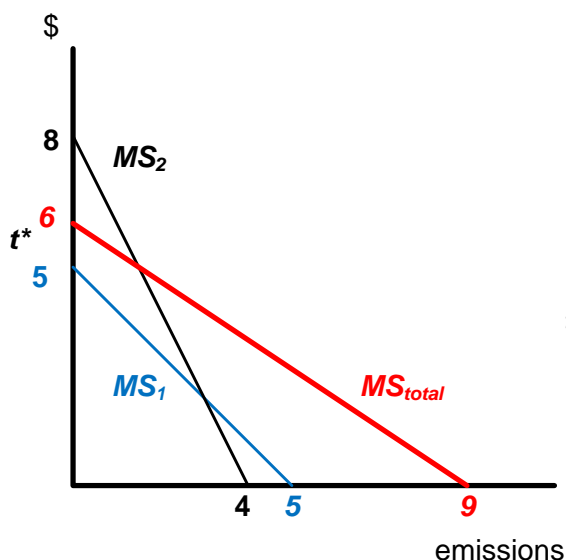
To aggregate re-write each as  $e_1 = 5 - MS$  and  $e_2 = 4 - 0.5MS$

$$(e_1 + e_2) = e = 9 - 1.5MS \text{ or } MS = 6 - 0.67e$$

Aggregate MD, add vertically:  $MD_1 + MD_2 = MD = 2e$

$$MD = MS \Rightarrow 2e = 6 - 0.67e \quad 2.67e = 6 \quad e^* = 2.25$$

The optimal tax is where  $MD = MS$  or  $t^* = 4.4$



## pg 259 #4 (chapter 12)

**F** be Fireyear and **G** be Goodstone

Total pollution emissions generated are  $E_F + E_G = Q_F + Q_G$ . The marginal damage of pollution is constant per unit of  $E$  at \$12

(a)  $G: 60(30) - 500 - (30)^2 = 400$

(b) Apply tax to firm's MC:  $MC_{NEW} = MC + t$

$$P = MC + t \quad F: 60 = 4Q_F + 12, \quad Q_F = 12 \quad G: 60 = 2Q_G + 12, \quad Q_G = 24$$

$$\text{Profits (after tax)} \quad P \times Q - TC - tQ$$

$$F: 60(12) - 300 - 2(12)^2 - 12(12) = -12$$

$$G: 60(24) - 500 - (24)^2 - 12(24) = 76$$

- (c) Profits(after subsidy, s)  $PxQ - TC + s(Q_a - Q_b) = PxQ - TC + sQ_a - sQ_b$  Where  $Q_a$  is output from part (a) and  $Q_b$  is output from part (b)

*From the book and lecture, we know optimal subsidy equals optimal tax. For every unit of output the firm adds a unit of emissions to the environment. Therefore the subsidy is a "cost" in terms of opportunity cost, thus*

$P = MC + s$  is the profit max rule. Since  $s = t = 12$ , output under subsidy is the same as (b)

$$F: 60(12) - 300 - 2(12)^2 - 12(12) + [15 \times 12] = -12 + 180 = 168$$

$$G: 60(24) - 500 - (24)^2 - 12(24) + [30 \times 12] = 76 + 360 = 436$$

- (d) *Under the tax policy, Fireyear will exit the market in the long run. Under the subsidy, both firms will remain. There may be entry into the market due to the subsidy unless there are barriers to entry.*

**pg 260 #5 Chapter 12**

$$P = 10 \quad C = Q^2 \quad E = 2Q$$

$$MD = 2 \text{ per } E \quad TD = 2E = 4Q$$

$$(a) \pi = TR - TC = 10Q - Q^2 - 4Q \quad \pi' = 10 - 2Q - 4 = 0 \quad Q = 3 \quad \pi = 9$$

$$(b) Q = E \quad \pi = TR - TC = 10Q - Q^2 - 2Q \quad \pi' = 10 - 2Q - 2 = 0 \quad Q = 4 \quad \pi = 16 \quad \Delta\pi = 7$$

$$(c) Q = 5 \quad \pi = 25$$

**Handout Question 1**

Suppose that the  $MD = 5E$  and with its current technology, the firm's MS is given by

$$MS_1 = 200 - 5E.$$

- Determine the socially optimal level of emissions  $E$ .  
 $200 - 5E = 5E$ , therefore  $E = 20$
- Determine the emissions tax that would achieve the socially optimal level of emissions.  
 $\text{Tax, } t = MS = 200 - 5E = 200 - 5(20) = 100$

Now suppose the firm can adopt a new technology that changes its MS to

$$\text{New } MS_2 = 160 - 4E$$

Calculate change in costs for the firm from adopting the new technology when:

- The government uses an emissions standard equal to your answer in (a) above  
If Standard set at  $E = 20$ , Old Technology has a TAC = \$1000. New Technology has  $MS = 80$  and a TAC = 800. Savings from switching is \$200
- The government uses an emissions tax equal to your answer in (b)  
(Assume no change to standard or tax rate after the change in technology)

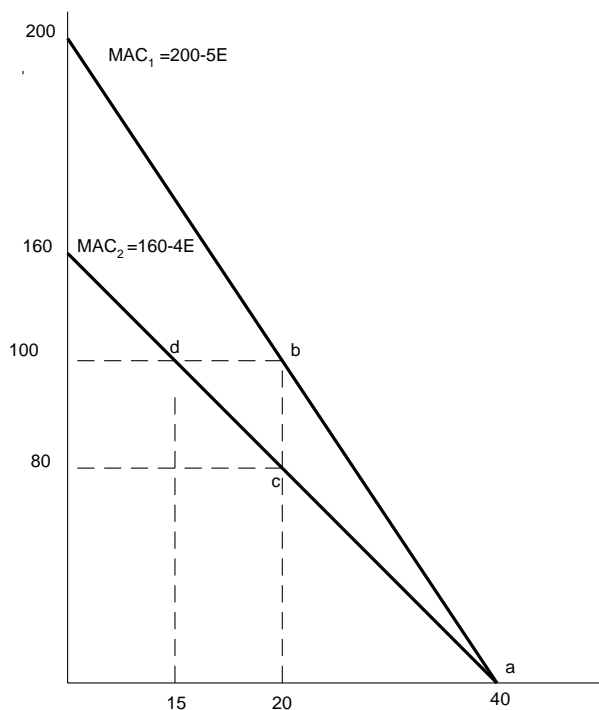
**With \$100 tax**

$$\text{Old: } MS_1 = 200 - 5E = 100 \text{ tax } E = 20$$

$$\text{New } MS_2 = 160 - 4E = 100 \text{ tax } E = 15$$

	Tech 1 (old)	Tech 2 (new)
TAC	$100 \times 20 \times (1/2) = 1000$	$25 \times 100 \times (1/2) = 1250$
TAX Bill	$100 \times 20 = 2000$	$100 \times 15 = 1500$
	\$3000	\$2750

**Savings from switching is \$250**



Now suppose the government adjusts the standard and/or the tax such that  $MD = \text{New MS}$ . Calculate the change in total costs for the firm from adopting the new technology when:

- e) The government adjusts the standard, and
- f) The government adjusts the tax rate

**Under NEW technology:**

$$MS_2 = MD$$

$$160 - 4E = 5E$$

$$E = 17.8 \text{ and } MS = 88.9$$

**With a standard equal to 17.8**

$$TAC = (40 - 17.8)(88.9) \cdot (1/2) = 986.8$$

$$\text{Savings} = 1000 - 986.8 = 13.2$$

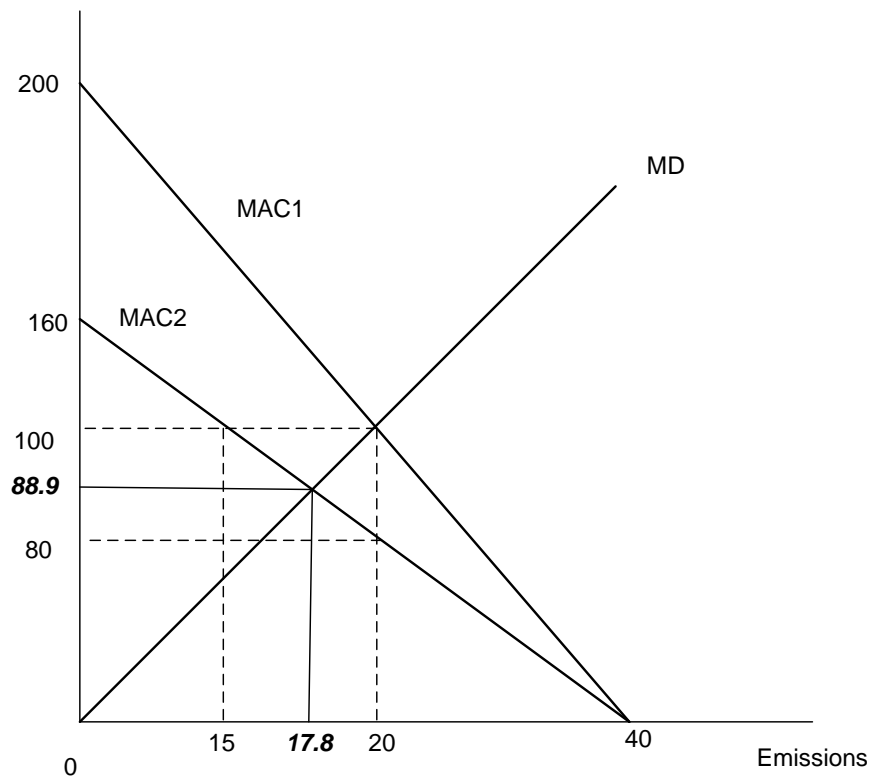
Under Tax rate of  $t = 88.9$ ,  $E = 17.8$

Tax bill =  $(88.9)(17.8) = 1582.4$

And TAC = 986.8

TAC + Taxbill = 2569.2

Savings =  $3000 - 2569.2 = 430.8$



Note in Graph:  $MAC_1$  is  $MS_1$  and  $MAC_2$  is  $MS_2$